

# HILDA Standard Errors

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# Outline

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- Hilda survey design
- Methods
- Design issues
- Preliminary results
- Improvements/Additions
- Benchmarking
- Final points

# HILDA Survey Design

- Australia was stratified via major statistical region
  - Census Collection Districts (CCD's) were systematically selected (via serpentine ordering)
  - probability of selection proportional to the number of dwellings in each CCD
- Dwellings were selected systematically from within CCD's
- Households were randomly selected within dwellings
- All individuals were selected in each household.

# SRS?

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- HILDA has a complex survey design with unequal weights
- Cluster selection causes groups of similar households to appear in the data
- People are clustered within households
- SRS formulas ignore clustering and the systematic selection

# Methods of Complex SE Calculation

- Method categories:
  - Linearisation techniques
  - Resampling
- HILDA user manual recommends only two:
  - Taylor Series Linearisation
  - Delete a group Jackknife

# Delete-a-group Jackknife

- The Jack-knife is a method for producing replicate weights for the sample
- 30 replicates provided for all weights on the dataset.
- Takes into account the complex design of the survey and the way it has evolved from wave 1
- Simple formula for the variance using the replicate weights

$$Var(\hat{x}) = \left( \frac{R-1}{R} \right) \sum_{r=1}^R \left( \hat{x}^{(r)} - \hat{x} \right)^2$$

# Delete-a-group Jackknife – Replicates

- Aim to mirror the overall sample design within each replicate group
- Ordered CCD's systematically allocated to a replicate group
  - CCD 1 to 30 allocated to replicate group 1 to 30 then repeated
- Allocated group of CCD's dropped from each replicate
  - Replicate group size 29/30 of main sample
- Replicate group undergoes weighting process
  - units in dropped CCD's receive zero weight

# Taylor Series Linearisation

- Use Taylor's Theorem to create a linear approximation to a non-linear statistic
- Calculate the variance of the linear approximation
- Benefits
  - Well developed theory
  - Can be applied in general sample designs
  - Software readily available
- Accuracy of linear approximation a concern

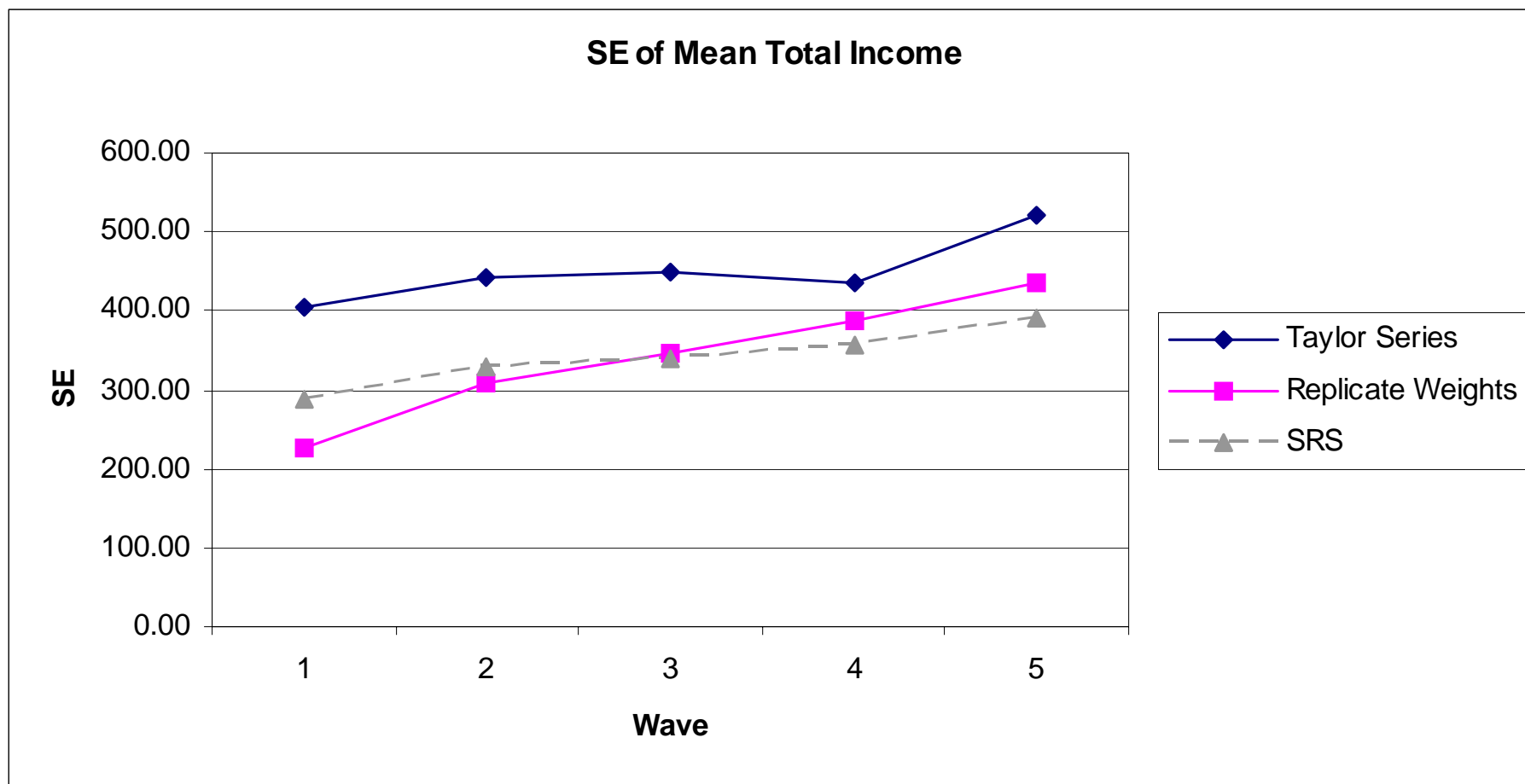
# Sample Design Issues

- Taylor Series
  - Software packages assume a stratified cluster design
  - Doesn't take into account benchmarking effects or systematic selection
- Replicate groups don't correctly reflect the sample design
  - Cluster size needs to be taken into account
  - Systematic selection skips

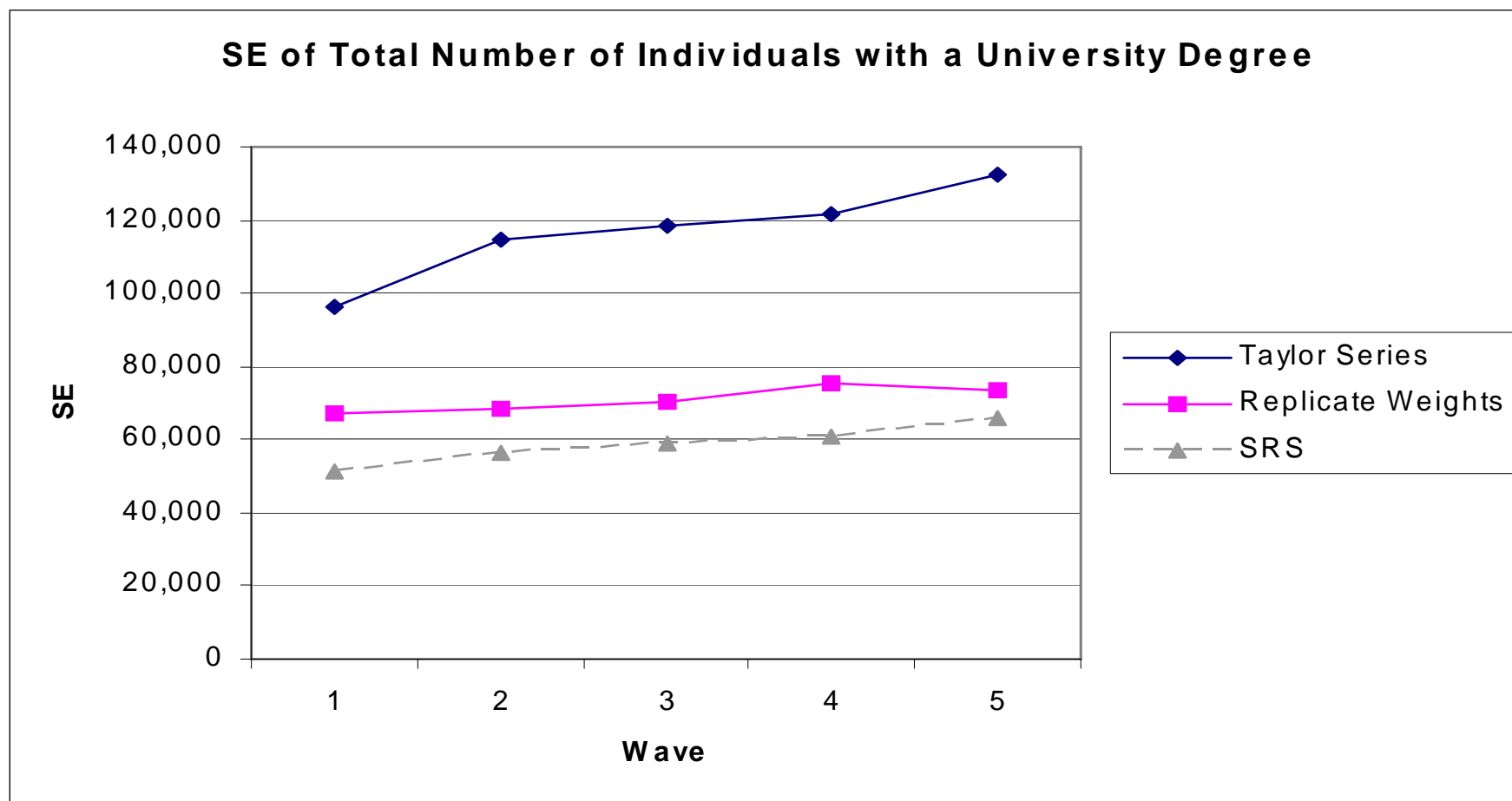
# Sample Design Issues

- As the survey progresses over time:
  - Systematic design less apparent
  - Sample dispersion/un-clustering
  - Unlikely to reduce to a random ordering of units
  - Approximation or replicate weights still more suitable than SRS

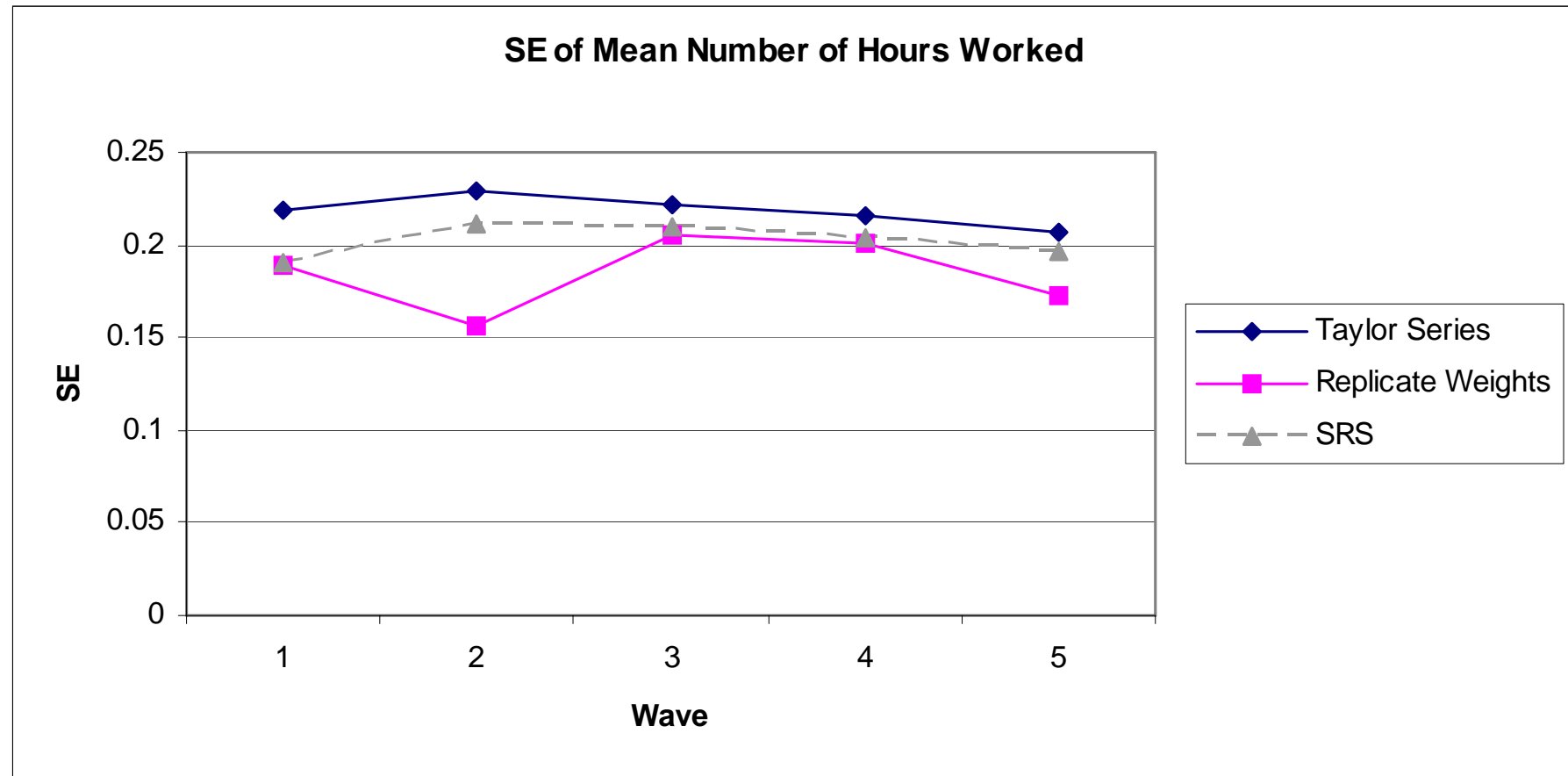
# Preliminary Results



# Preliminary Results



# Preliminary Results



# Observations

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- Large difference between methods
- What is correct?
- Increase in estimates over waves
  - Attrition
  - Un-clustering
  - New sample members

# Updated Taylor Series estimates

- Taylor approximation method only using a broad stratification variable
- Choose finer level stratum boundaries
  - Closer approximation to the systematic selection
- Incorporate the original ordering of the clusters

# Updated Taylor Series estimates

| <b>Revised Stratum Variable</b> | <i>W 1</i> | <i>W 2</i> | <i>W 3</i> | <i>W 4</i> | <i>W 5</i> |
|---------------------------------|------------|------------|------------|------------|------------|
| <i>Average Income</i>           |            |            |            |            |            |
| Major statistical Region        | 405        | 442        | 450        | 436        | 521        |
| CD order strata                 | 385        | 413        | 428        | 423        | 493        |
| <i>Average Hours</i>            |            |            |            |            |            |
| Major statistical Region        | 0.2186     | 0.2299     | 0.2219     | 0.2164     | 0.2064     |
| CD order strata                 | 0.2188     | 0.2335     | 0.2215     | 0.2131     | 0.1995     |
| <i>Education Count</i>          |            |            |            |            |            |
| Major statistical Region        | 96,326     | 114,547    | 118,612    | 121,871    | 132,278    |
| CD order strata                 | 85,054     | 89,868     | 91,915     | 93,347     | 102,099    |

# Updated Replicate Estimates W1 (1)

- Introduced the replicate weight creation at the start of the weighting process
- Small change in results

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## Replicate Weights Comparison - Wave 1

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|                        | <i>Existing Replicates</i> | <i>Adjusted Replicates</i> |
|------------------------|----------------------------|----------------------------|
| <i>Average Income</i>  | 226                        | 214                        |
| <i>Average Hours</i>   | 0.1884                     | 0.1975                     |
| <i>Education Count</i> | 66,937                     | 70,123                     |

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# Replicate Group Formation

- Updated to take into account the size of each cluster
- Random start point with systematic selection of clusters for each replicate
  - Random number has a very large impact on results
  - Larger number of replicate improves consistency across runs

# Updated Replicate Estimates W1 (2)

| <i>Mean Income SE</i>       |             |                      | Original<br>Replicates |
|-----------------------------|-------------|----------------------|------------------------|
| <i>Replicates</i>           | <i>Mean</i> | <i>Std Deviation</i> |                        |
| 30                          | 276         | 49                   | 214                    |
| 100                         | 276         | 23                   |                        |
| <i>Mean Hours worked SE</i> |             |                      | 0.198                  |
| <i>Replicates</i>           | <i>Mean</i> | <i>Std Deviation</i> |                        |
| 30                          | 0.185       | 0.021                | 0.198                  |
| 100                         | 0.180       | 0.013                |                        |
| <i>Education Count SE</i>   |             |                      | 70,123                 |
| <i>Replicates</i>           | <i>Mean</i> | <i>Std Deviation</i> |                        |
| 30                          | 65,400      | 6,519                | 70,123                 |
| 100                         | 65,096      | 8,136                |                        |

# HILDA Benchmarking

- Benchmarking reduces estimates of SE via replicate weights for related variables
- Incorporate the error of survey benchmarks?

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*HILDA survey Benchmark source*

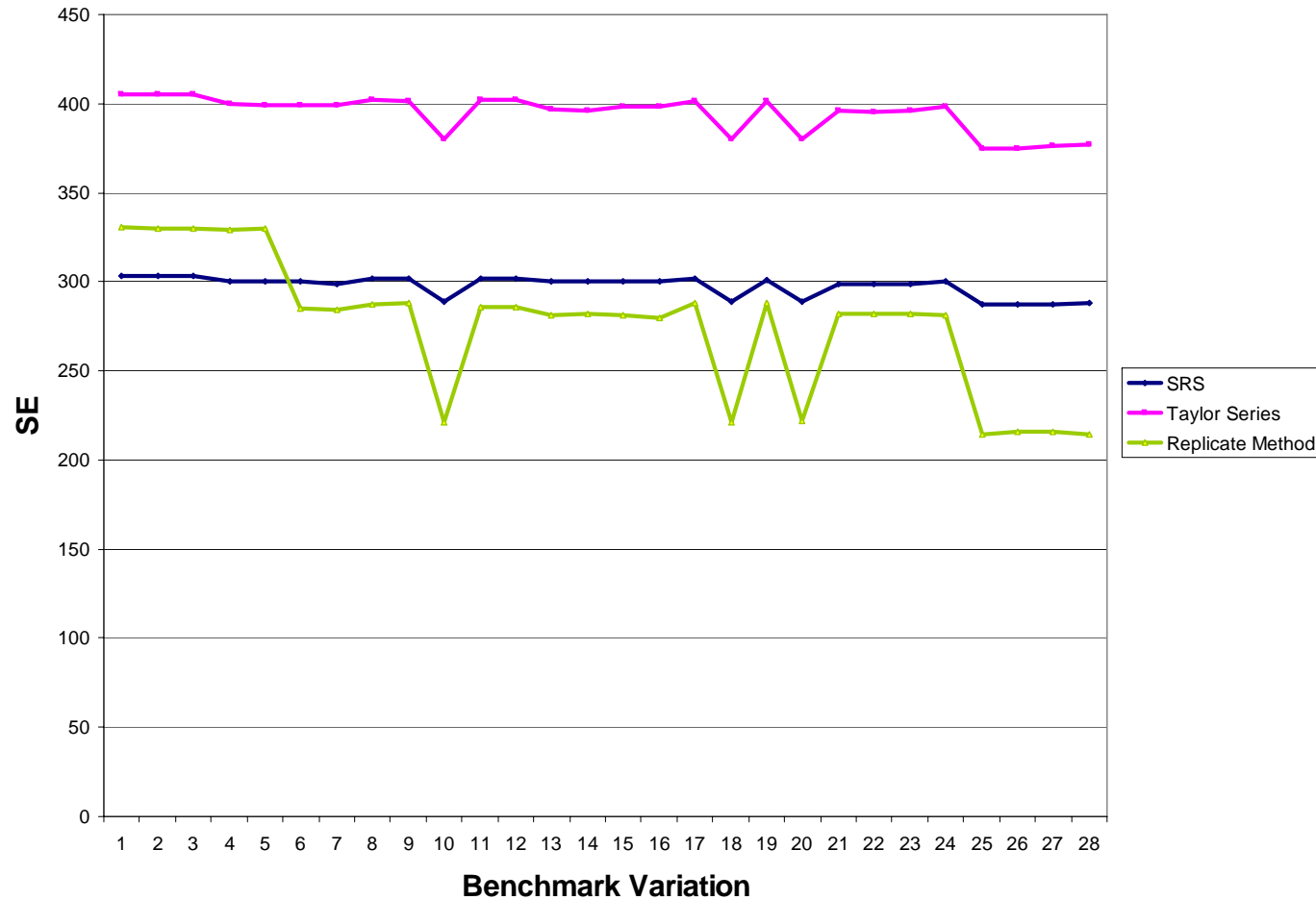
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| <i>Estimated Residential Population</i> | <i>Labour Force Survey</i> |
|---|----------------------------|
| Number of Adults                        | Labour Force Status        |
| Number of Children                      | Social Marital Status      |
| Broad State Group                       | Occupation                 |
| State                                   |                            |
| Capital City                            |                            |
| Sex                                     |                            |
| Age Group                               |                            |

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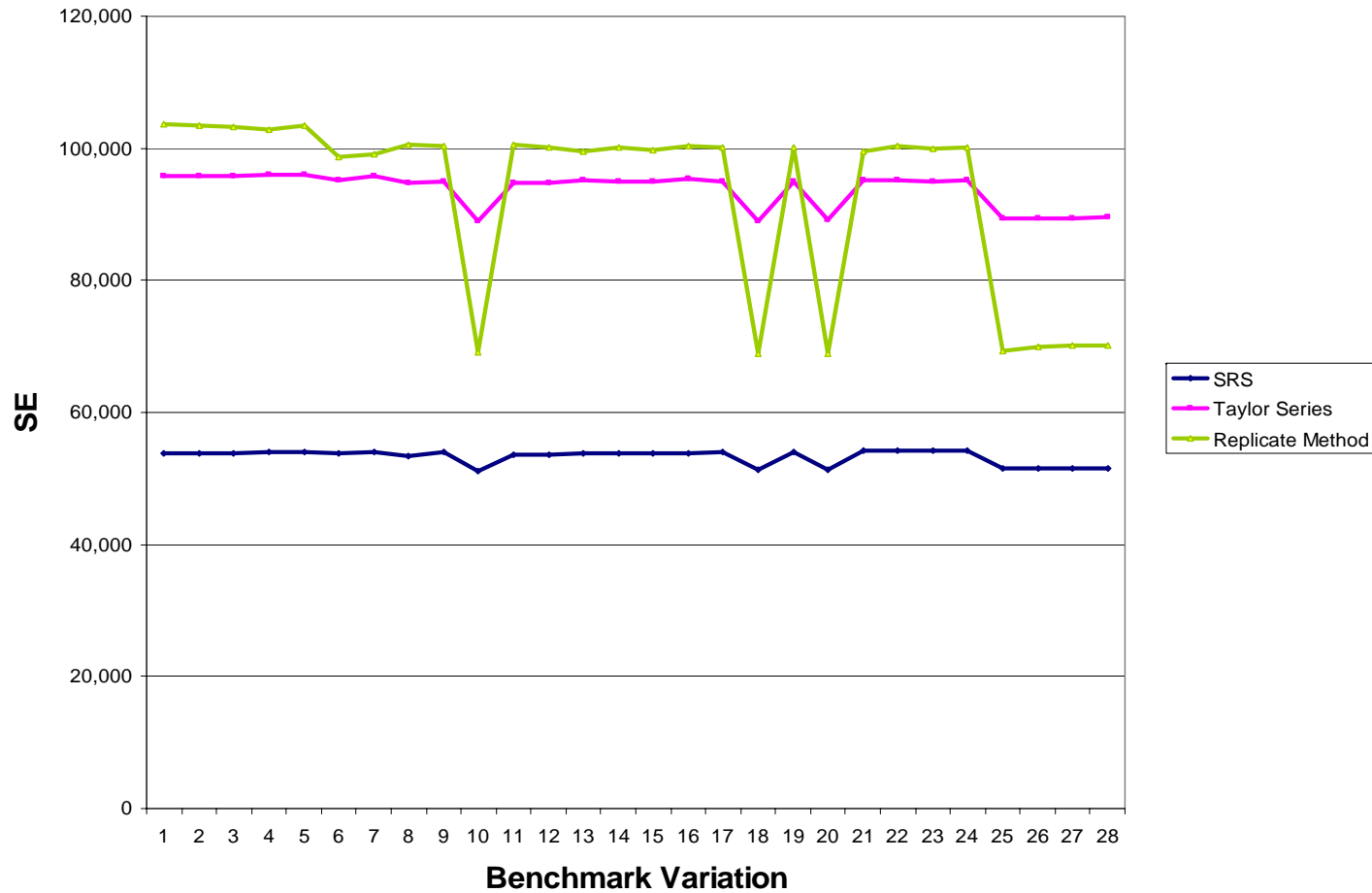
# Effect of benchmarking on estimates

Average Income SE - method comparison



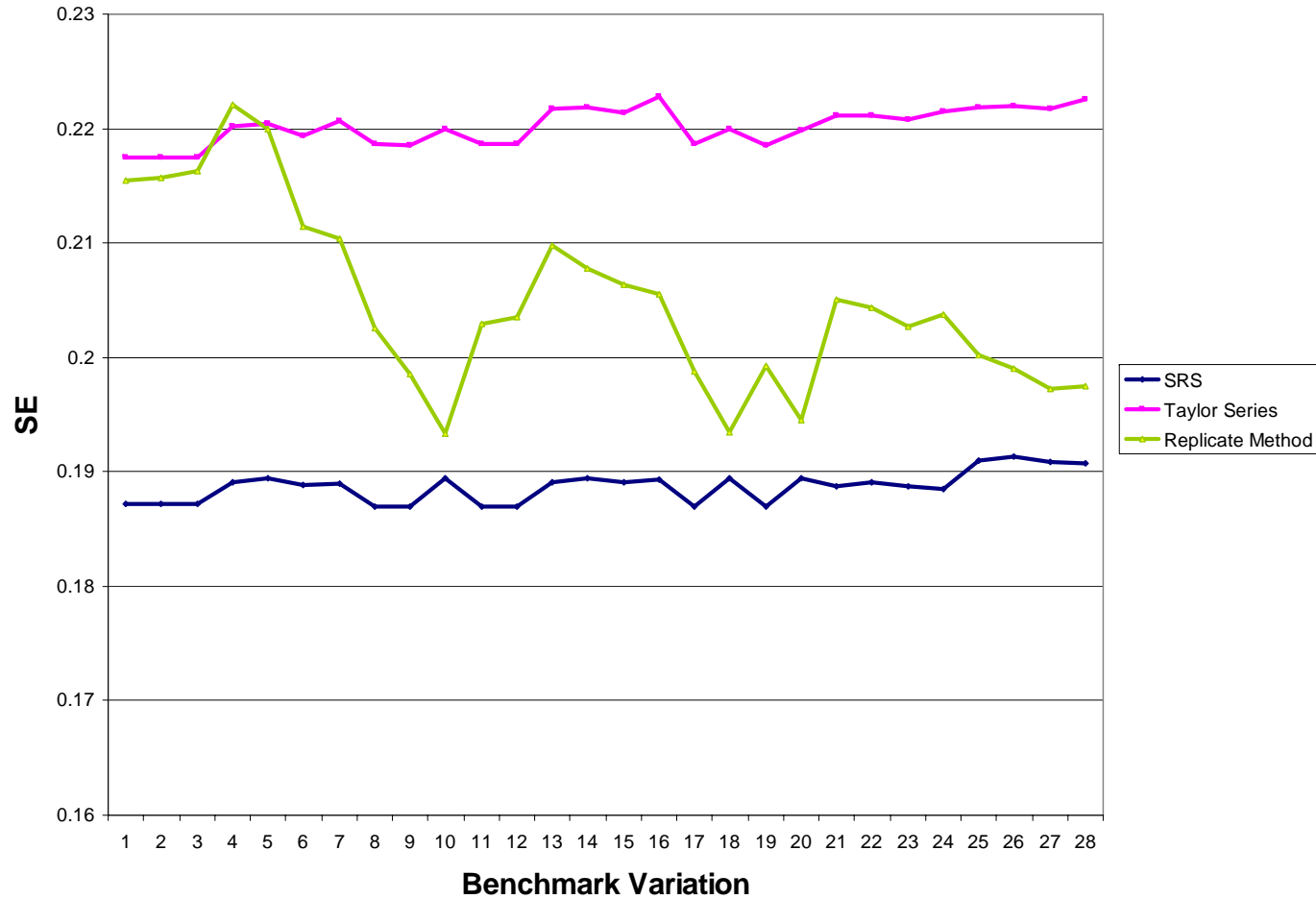
# Effect of benchmarking on estimates

Education Count SE - Method Comparison



# Effect of benchmarking on estimates

Average Hours SE - Method Comparison



# Observations

- Large drop in the replicate estimate:
  - As more benchmarks are added
  - When the labour force survey benchmarks are introduced
- Incorporate error into external benchmarks from the Labour force survey due to their impact on estimates
- Overall should we benchmark to less?

# Potential changes to HILDA Release 6

- Provide the updated stratification variable for the Taylor Series method
- Replicate weights
  - Update the replicate group selection process
  - Implement from the start of the weighting process
  - Add error to the LFS benchmarks
  - Provide more replicates?

# Future work

- More investigation:
  - Sample design effect
  - Current recommended methods
- Alternative methods
  - Group Bootstrap
- Discussion paper to go on the website
  - <http://www.melbourneinstitute.com/hilda/>